

The Informath Deployment Stack

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Informath

NextReason
MALINCA



European Research Council
Established by the European Commission

Informath

The ultimate syntactic sugar: ordinary mathematical language

```
Thm04 : (u : Elem Vector) -> (v : Elem Vector) ->  
  Proof (orthogonal u v) ->  
    Proof (Eq Real (length (vectorPlus u v))  
      (sqrt (plus (square (length u)) (square (length v)))))).
```

Thm04. For all vectors u and v , if $u \perp v$, then

$$\|u + v\| = \sqrt{\|u\|^2 + \|v\|^2}.$$

Variations in ordinary mathematical language

```
Thm04 : (u : Elem Vector) -> (v : Elem Vector) ->  
  Proof (orthogonal u v) ->  
    Proof (Eq Real (length (vectorPlus u v))  
      (sqrt (plus (square (length u)) (square (length v)))))).
```

```
$ RunInformath -variations tmp/t4.dk | wc -l  
2542
```

Thm04. For all vectors u and v , if $u \perp v$, then

$$\|u + v\| = \sqrt{\|u\|^2 + \|v\|^2}.$$

Thm04. Let u and v be vectors. Assume that u is orthogonal to v . Then the length of the sum of u and v is equal to the square root of the sum of the square of the length of u and the square of the length of v .

Scoring and ranking alternative phrases

```
data Scores = Scores {  
  tree_length :: Int,  
  tree_depth  :: Int,  
  characters   :: Int,  
  tokens       :: Int,  
  subsequent_dollars :: Int,  
  initial_dollars  :: Int,  
  extra_pauses   :: Int  
}
```

These all are penalties

- minimize some linear combination of them
- users can give weights to each score (default = 1)

Uses of informalization

Documenting formal mathematics

- Useful for documenting formal mathematics (Coscoy et al. 1994)

Formalizing informal mathematics

- via parsing with reversible grammars (CNL approach)
- via generating synthetic data for neural models (Wang et al. 2018)

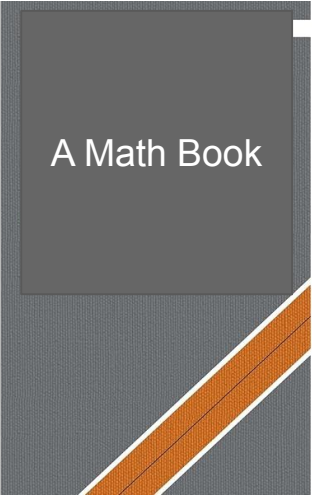
Uses of informalization

Documenting formal mathematics

- Useful for documenting formal mathematics (Coscoy et al. 1994)
- Indispensable for explaining AI generated code (Urban et al. 2026)

Formalizing informal mathematics

- via parsing with reversible grammars (CNL approach)
- via generating synthetic data for neural models (Wang et al. 2018)



A Math Book

LLM autoformalization

```
t0 a (t0 b c)) (t0 (t0 a b) c)) => match_Aop a1
a2 (plus Type2 (nd 1)) (___ : Aop a1 a2 => univ
Type2) (u0 : (___ : a1 -> __1 : a1 -> a1) => u1
: (a : a1 -> Eq (u0 a2 a) a) => u2 : (a : a1 ->
Eq (u0 a a2) a) => u3 : (a : a1 -> b : a1 -> c
: a1 -> Eq (u0 a (u0 b c)) (u0 (u0 a b) c)) =>
prod (plus Type1 (nd 1)) Type1 (univ Type1) (P
: Type1 => prod Type1 Type1 (prod Prop Type1
(Eq (R0 (prod Set Set a1 (___ : a1 => prod Set
Set a1 (___1 : a1 => a1))) t0) u0) (e0 : Eq (R0
(prod Set Set a1 (___ : a1 => prod Set Set a1
(___1 : a1 => a1))) t0) u0 => prod Prop Type1
(Eq (R1 (prod Set Set a1 (___ : a1 => prod Set
Set a1 (___1 : a1 => a1))) t0 (x_19 : (___ : a1
-> __1 : a1 -> a1) => _x_20 : Eq t0 x_19 => (x0
: (___ : a1 -> __1 : a1 -> a1) => p0 : Eq t0 x0
=> prod Set Prop a1 (a : a1 => Eq (x0 a2 a) a))
x_19 _x_20) t1 u0 e0) u1) (e1 : Eq (R1 (prod
Set Set a1 (___ : a1 => prod Set Set a1 (___1 :
a1 => a1))) t0 (x_19 : (___ : a1 -> __1 : a1 ->
a1) => _x_20 : Eq t0 x_19 => (x0 : (___ : a1 ->
__1 : a1 -> a1) => p0 : Eq t0 x0 => prod Set
Prop a1 (a : a1 => Eq (x0 a2 a) a)) x_19 _x_20)
t1 u0 e0) u1 => prod Prop Type1 (Eq (R2 (prod
Set Set a1 (___ : a1 => prod Set Set a1 (___1 :
a1 => a1))) t0 (x0 : (___ : a1 -> __1 : a1 ->
a1) => ___ : Eq t0 x0 => (x01 : (___1 : a1 -> __2
: a1 -> a1) => p0 : Eq t0 x01 => prod Set Prop
a1 (a : a1 => Eq (x01 a2 a) a)) x0 ___) t1 (x0 :
(___ : a1 -> __1 : a1 -> a1) => p0 : Eq t0 x0 =>
x1 : (x01 : (___ : a1 -> __1 : a1 -> a1) => p01
: Eq t0 x01 => prod Set Prop a1 (a : a1 => Eq
(x01 a2 a) a)) x0 p0 => ___ : Eq (R1 (prod Set
Set a1 (___ : a1 => prod Set Set a1 (___1 : a1 =>
```

A Math Book

LLM autoformalization

```
t0 a (t0 b c)) (t0 (t0 a b) c)) => match_Aop a1
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Type2) (u0 : (___ : a1 -> ___1 : a1 -> a1) => u1
: (a : a1 -> Eq (u0 a2 a) a) => u2 : (a : a1 ->
Eq (u0 a a2) a) => u3 : (a : a1 -> b : a1 -> c
: a1 -> Eq (u0 a (u0 b c)) (u0 (u0 a b) c)) =>
prod (plus Type1 (nd 1)) Type1 (univ Type1) (P
: Type1 => prod Type1 Type1 (prod Prop Type1
(Eq (R0 (prod Set Set a1 (___ : a1 => prod Set
Set a1 (___1 : a1 => a1)))) t0) u0) (e0 : Eq (R0
(prod Set Set a1 (___ : a1 => prod Set Set a1
(___1 : a1 => a1)))) t0) u0 => prod Prop Type1
(Eq (R1 (prod Set Set a1 (___ : a1 => prod Set
Set a1 (___1 : a1 => a1)))) t0 (x_19 : (___ : a1
-> ___1 : a1 -> a1) => x_20 : Eq t0 x_19 => (x0
: (___ : a1 -> ___1 : a1 -> a1) => p0 : Eq t0 x0
=> prod Set Prop a1 (a : a1 => Eq (x0 a2 a) a))
x_19_x_20) t1 u0 e0) u1) (e1 : Eq (R1 (prod
Set Set a1 (___ : a1 => prod Set Set a1 (___1 :
a1 => a1)))) t0 (x_19 : (___ : a1 -> ___1 : a1 ->
a1) => x_20 : Eq t0 x_19 => (x0 : (___ : a1 ->
___1 : a1 -> a1) => p0 : Eq t0 x0 => prod Set
Prop a1 (a : a1 => Eq (x0 a2 a) a)) x_19_x_20)
t1 u0 e0) u1 => prod Prop Type1 (Eq (R2 (prod
Set Set a1 (___ : a1 => prod Set Set a1 (___1 :
a1 => a1)))) t0 (x0 : (___ : a1 -> ___1 : a1 ->
a1) => ___ : Eq t0 x0 => (x01 : (___1 : a1 -> ___2
: a1 -> a1) => p0 : Eq t0 x01 => prod Set Prop
a1 (a : a1 => Eq (x01 a2 a) a)) x0 ___) t1 (x0 :
(___ : a1 -> ___1 : a1 -> a1) => p0 : Eq t0 x0 =>
x1 : (x01 : (___ : a1 -> ___1 : a1 -> a1) => p01
: Eq t0 x01 => prod Set Prop a1 (a : a1 => Eq
(x01 a2 a) a)) x0 p0 => ___ : Eq (R1 (prod Set
Set a1 (___ : a1 => prod Set Set a1 (___1 : a1 =>
```

symbolic
informalization

Thm03. $\mathbb{Q}$ is denumerable.

Thm03a.

$$|N| = |\mathbb{Q}|.$$

Thm04. Let u and v be vectors. Then $u \perp v$ implies $\|u + v\| = \sqrt{\|u\|^2 + \|v\|^2}$.

Thm07. Let $p, q \in \mathbb{N}$. Then if p and q are prime, then

$$\binom{p}{q} \binom{q}{p} = (-1)^{\frac{p-1}{2} \frac{q-1}{2}}.$$

Thm09. Let c be a circle. Let r be a real number. Assume that $r = \text{radius}(c)$. Then the area of c is equal to $\pi \times r^2$.

Thm10FermatLittle. Let p be a natural number. Assume that p is prime. Let a be an integer. Then there exists an integer q , such that $a^p - a = p \times q$.

Thm11. $p \geq n$ and p is prime for a natural number p for all natural numbers n .

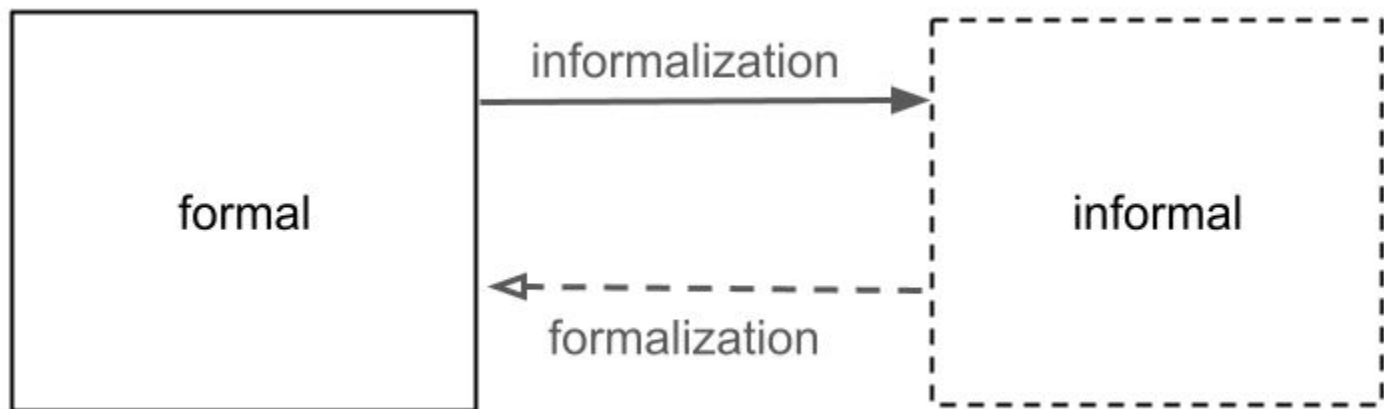
Thm19. $n = a^2 + b^2 + c^2 + d^2$ for some natural numbers a, b, c and d for all natural numbers n .

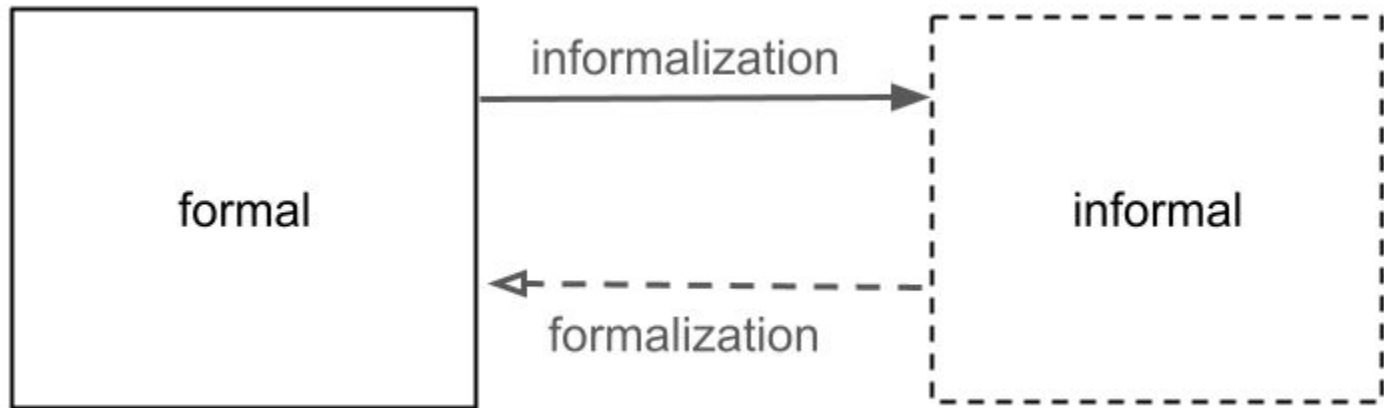
Thm20a. Let p be a natural number. Assume that p is prime. Let k be a natural number. Assume that $p = 4 \times k + 1$. Then there exists a natural number x , such that there exists a natural number y , such that $p = x^2 + y^2$.

Thm20b. Let p be a natural number. Assume that p is prime. Assume that $p \equiv 1 \pmod{4}$. Then there exists a natural number x , such that there exists a natural number y , such that $p = x^2 + y^2$.

Thm22. It is not the case that $\mathbb{R}$ is denumerable.

Mock-up example: the code and the text do not correspond to each other.





formal language

- precisely defined
- possible to check
- possible to cover completely

LLM formalization

- complete coverage
- results can be checked

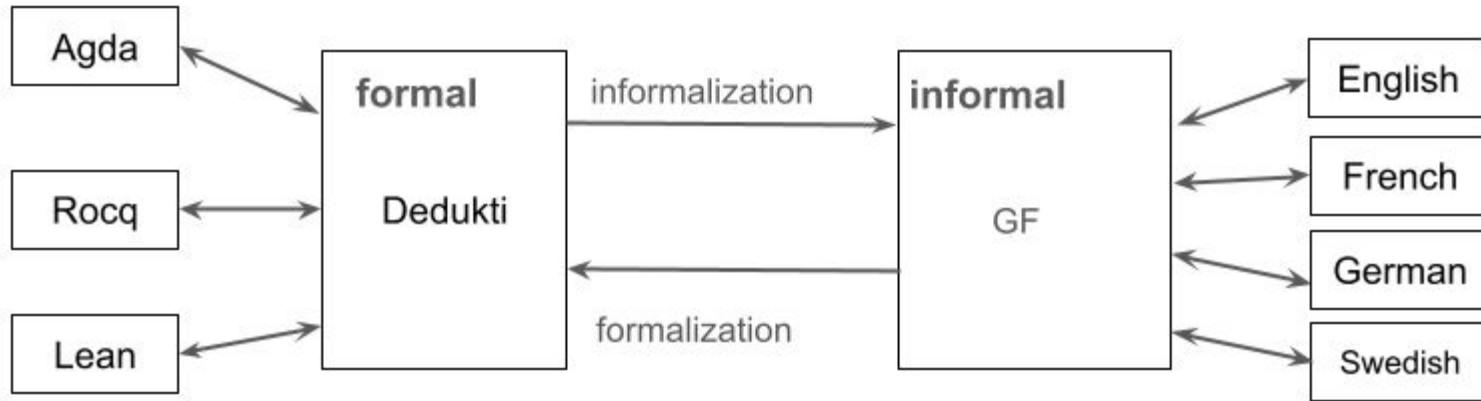
rule-based informalization

- complete coverage
- correct by construction

informal language

- not precisely defined
- not possible to check
- impossible to cover completely

The project Informath: structure



<https://www.grammaticalframework.org/>
<https://github.com/GrammaticalFramework/informath>

The project Informath: goals

Semantic completeness: everything expressible in type theory can be translated to Informath natural language.

Semantic soundness: everything expressible in Informath can be translated to type theory.

Linguistic completeness: everything attested in mathematical texts should be eventually covered by Informath.

Linguistic soundness: nothing should be added to Informath unless it is attested in mathematical texts.

Some statistics

Syntax rules: ~ 200 GF functions, extends to 87,000 BNF rules in English

Lexicon: ~ 4000 items, around 11,000 word forms in English

Languages: English, French, German, Swedish (common abstract syntax, implemented with a functor over GF Resource Grammar API)

Formalisms: Dedukti; Agda, Lean, Rocq ; Megalodon and Mizar forthcoming

Examples:

- arithmetic, algebra, set theory, topology, a sample of Wiedijk's "100 theorems", homotopy type theory;
- Dedukti dumps from Lean, Matita, Megalodon, Agda

Restrictions: proofs still very rudimentary

The Informath deployment stack

Out of the box

Light-weight annotations, no recompilation

Adding new words

Adding new syntax and semantics

Linguistic details

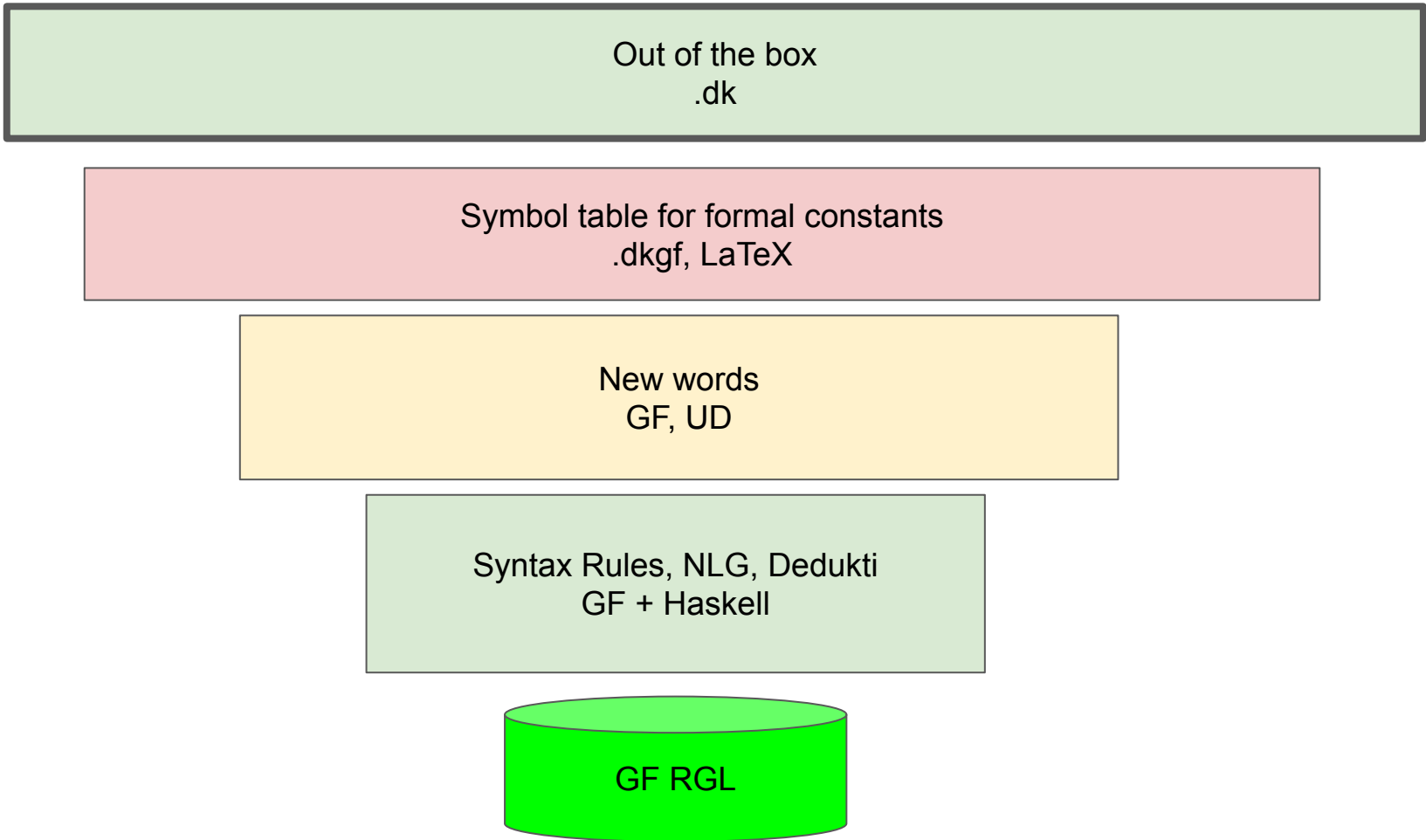
Out of the box
.dk

Symbol table for formal constants
.dkgf, LaTeX

New words
GF, UD

Syntax Rules, NLG, Dedukti
GF + Haskell

GF RGL



Out of the box
.dk

Symbol table for formal constants
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New words
GF, UD

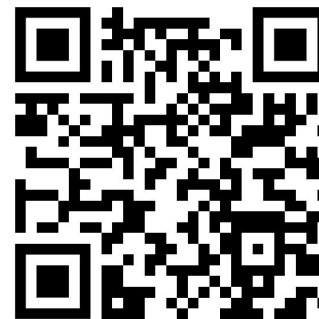
Syntax Rules, NLG, Dedukti
GF + Haskell

GF RGL

Installing Informath: binary

<https://github.com/GrammaticalFramework/informath>

<https://github.com/GrammaticalFramework/informath/releases>



Running the Informath binary: demo

```
$ make demo
```

Running the Informath binary: more demos

```
$ make sigma
```

```
$ make hott_demo
```

```
$ make naproche
```

```
$ make lang=Fre top100
```

Running the Informath binary: informalize a .dk file

```
$ RunInformath test/sets.dk
```

Running the Informath binary: inspect options

```
$ RunInformath -help
```


Running the Informath binary: some useful options

```
$ RunInformath -variations -nbest=11
```

```
$ RunInformath -to-latex-doc
```

```
$ RunInformath -to-lang=Fre
```

```
$ RunInformath -to-formalism=lean
```

Running the Informath binary: formalize a .tex file

```
$ RunInformath -test/naproche-zf-set.tex
```

Running the Informath binary on std-in

```
$ echo "c : Proof (exists Nat (n => divide n 7))." | RunInformath
```

```
$ echo "Every number is even or odd." | RunInformath -formalize
```

Running the Informath binary: analyse files

```
$ RunInformath -idents test/mini-matita.dk
```

```
$ RunInformath -unknown-idents test/mini-matita.dk
```

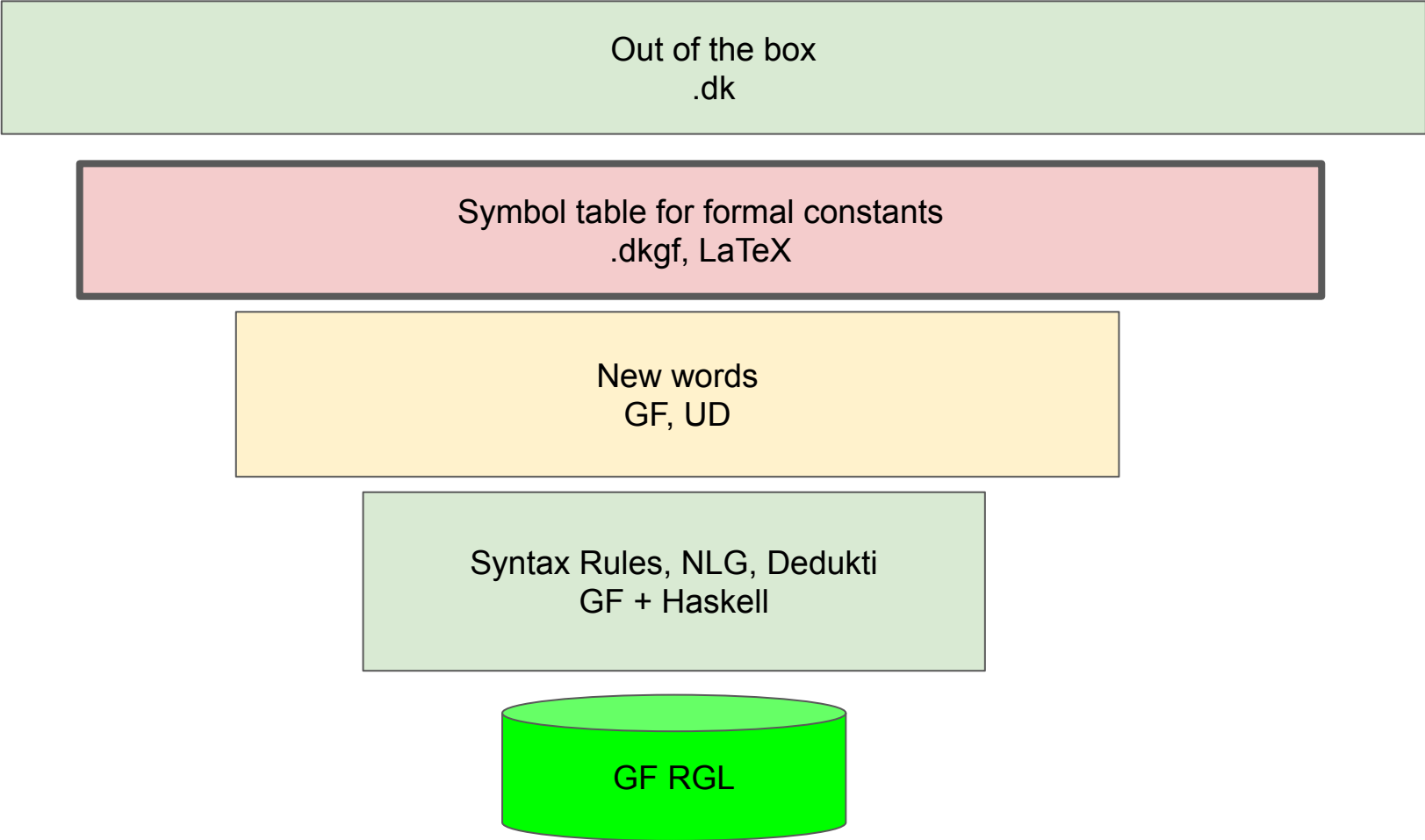
```
$ RunInformath-unknown-words ../rijke/rijke-tex/groups.tex
```

Running the Informath binary: select symbol tables

```
$ RunInformath test/hott_demo.dk
```

```
$ RunInformath -unknown-idents test/hott_demo.dk
```

```
$ RunInformath -symboltables=test/hott_demo.dkgf test/hott_demo.dk
```



Out of the box
.dk

Symbol table for formal constants
.dkgf, LaTeX

New words
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Syntax Rules, NLG, Dedukti
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GF RGL

Adapting to new concepts: symbol tables

```
-- file.dk
```

```
Div : Elem Nat -> Elem Nat -> Prop.
```

```
-- file.dkgf
```

```
Div: "X is divisible by Y" | $#2 \mid #1$
```

.dk

Div x 9

.tex

x is divisible by 9

$9 \mid x$

.dkgf

Div : "X is divisible by Y" | $\#2 \mid \#1$

GF abstract syntax and some derived structures

Eq: "X is divisible by Y" $\rightarrow$ divisible_Adj2

- *6 is not divisible by 4* not (Div 6 4)
- *6 and 9 are divisible by 3* and (Div 6 3) (Div 9 3)
- *x is even and divisible by 3* and (Even x) (Div x 3)
- *let n be a number divisible by 4* (n : Elem Nat) -> Proof (Div n 4) ->

Running the Informath binary: testing examples

```
$ echo "X is divisible by Y" | RunInformath -parse-example
```

```
$ echo "X is a principal ultrafilter" | RunInformath -parse-example
```

Checking symbol tables

```
$ RunInformath -base=test/maps.dk test/maps.dkgf
```

.dk

Div x 9

.tex

x is divisible by 9

$x \bmod 9$

.dkgf

Div : "X is divisible by Y" | $x \bmod y$

.gf abstract

fun

divisible_Adj : Adj

by_Prep : Prep

.gf English

lin

divisible_Adj = mkAdj "divisible"

by_Prep = RGL.by_Prep

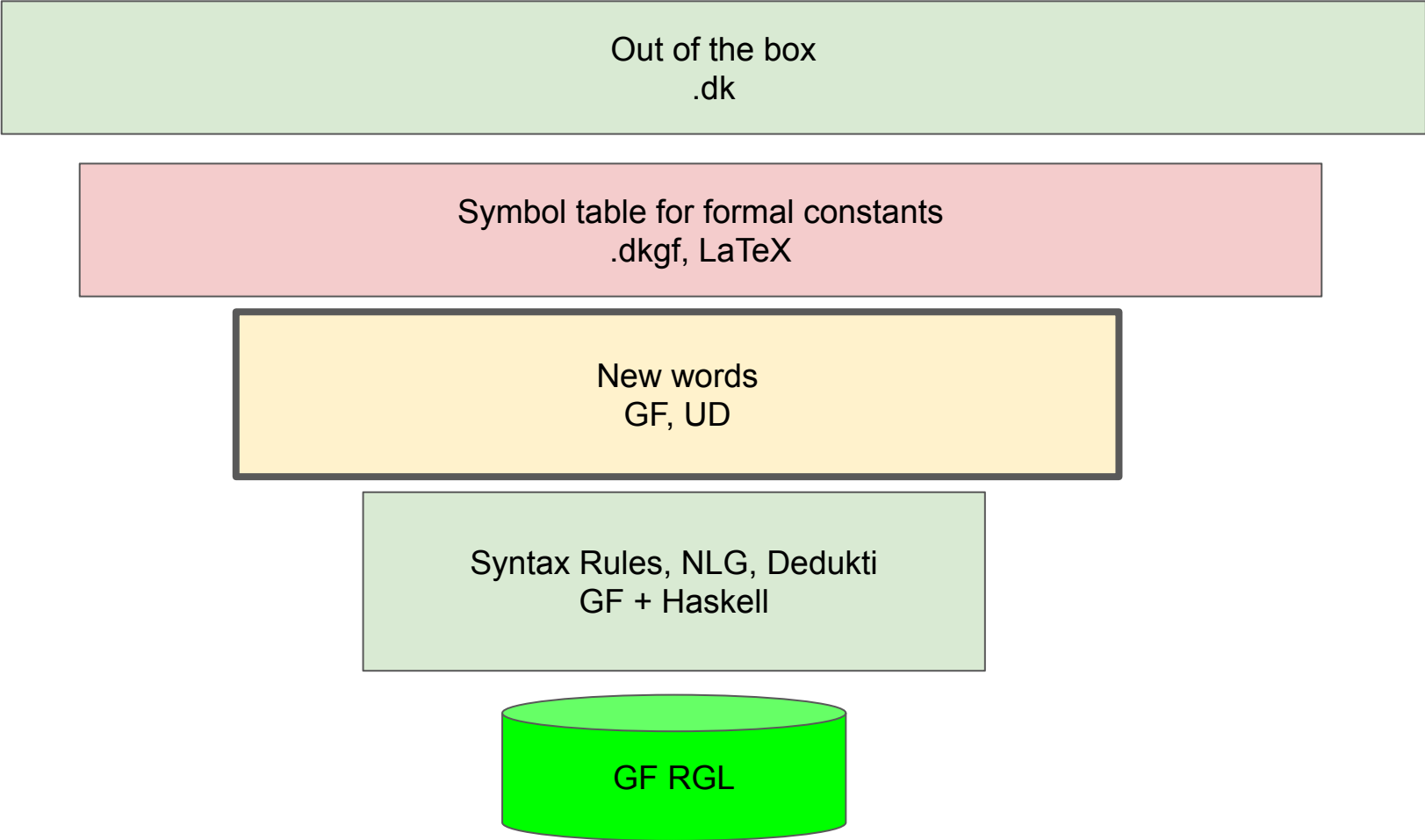
.gf German

divisible_Adj = mkAdj "teilbar"

by_Prep = RGL.by_Prep

divisible_Adj =

by_Prep = RGL.by_Prep



Out of the box
.dk

Symbol table for formal constants
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GF RGL

Manually in GF: files

```
abstract MyWords = Categories ** {  
  
  fun dictionary_Noun : Noun ;  
  fun explicit_Adj : Adj ;  
  fun put_Verb : Verb ;  
}
```

```
concrete MyWordsEng = CategoriesEng **  
  
open UtilitiesEng, ParadigmsEng, IrregEng in {  
  
  lin dictionary_Noun = mkNoun "dictionary" ;  
  lin explicit_Adj = mkAdj "explicit" ;  
  lin put_Verb = mkVerb put_V ;  
}
```

Manually in GF: files

```
abstract MyWords = Categories ** {  
  
  fun dictionary_Noun : Noun ;  
  fun explicit_Adj : Adj ;  
  fun put_Verb : Verb ;  
}
```

```
concrete MyWordsFre = CategoriesFre **  
open UtilitiesFre, ParadigmsFre, IrregFre in {  
  
  lin dictionary_Noun =  
    mkNoun "dictionnaire" masculine ;  
  lin explicit_Adj = mkAdj "explicite" ;  
  lin put_Verb = mkVerb mettre_V ;  
}
```

Include and recompile

```
abstract UserExtensions =  
  Categories,  
  Naproche,  
  NaprocheWords,  
  HottWords,  
  GodementWords,  
  NaturalDeduction,  
  ProofUnits,  
  MyWords  
;
```

```
concrete UserExtensionsEng of UserExtensions =  
  CategoriesEng,  
  NaprocheEng,  
  NaprocheWordsEng,  
  HottWordsEng,  
  GodementWordsEng,  
  NaturalDeductionEng,  
  ProofUnitsEng,  
  MyWordsEng  
;
```

```
$ make english_grammar
```

```
$ make multi_grammar
```


Running a script on a word list

```
# file adjs.txt  
explicit  
implicit  
elegant  
hard  
connected
```

```
$ python3 generate_gf.py Adj <adjs.txt
```

```
$ make multi_grammar
```

Preparing a word list from UD trees

```
# file godement.conllu

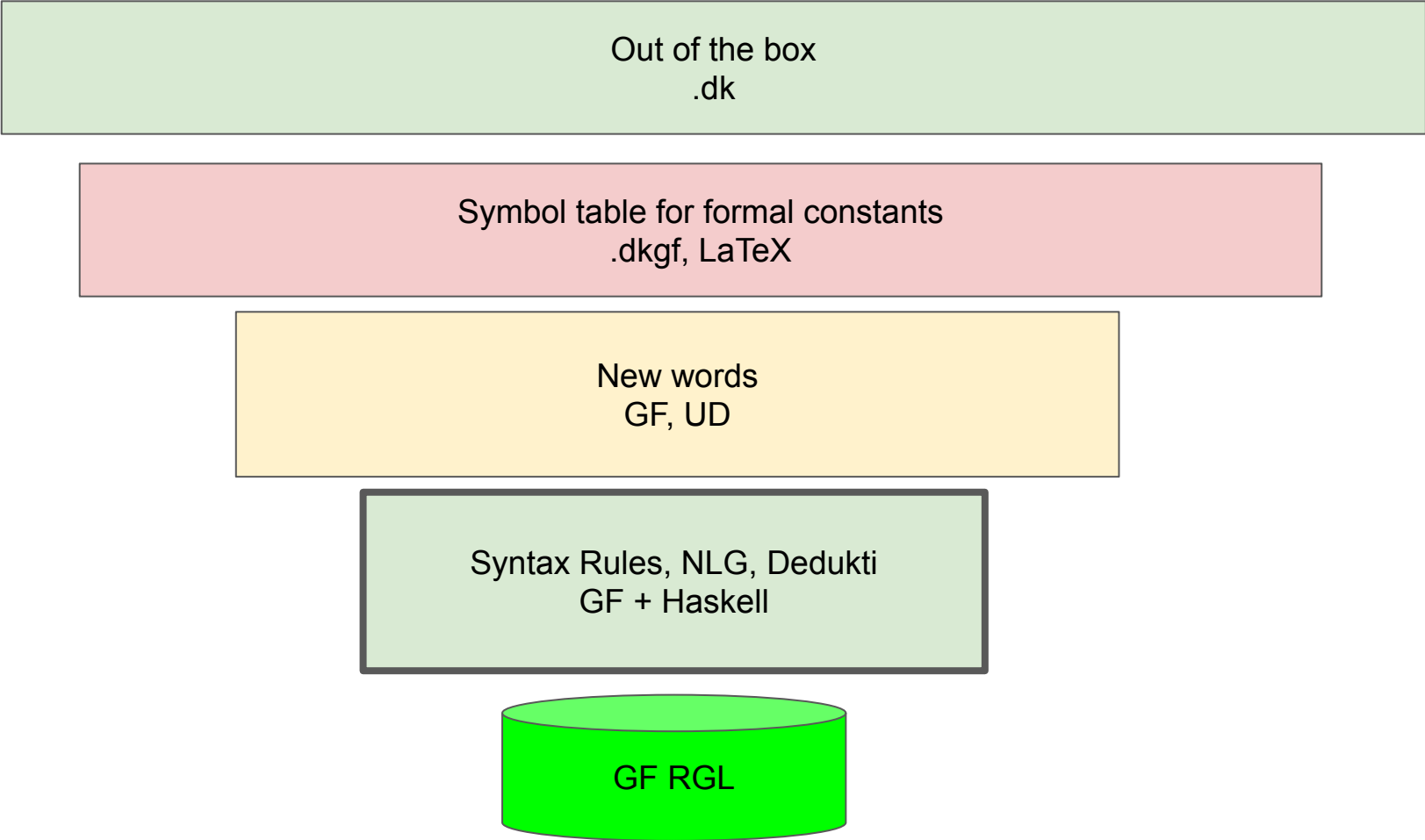
# text = Let LATEXMATH be elements of a principal ideal domain K .
1      Let      let      VERB    VB      Mood=Imp|VerbForm=Fin    0      root      _      SpacesAfter=\s\s
2      LATEXMATH      Latexmath      PROPN    NNP      Number=Sing    1      obj      _      SpacesAfter=\s\s
3      be      be      AUX      VB      VerbForm=Inf    4      cop      _      _
4      elements      element NOUN    NNS      Number=Plur    1      xcomp      _      _
5      of      of      ADP      IN      _      10      case      _      _
6      a      a      DET      DT      Definite=Ind|PronType=Art    10      det      _      _
7      principal      principal      ADJ      JJ      Degree=Pos    9      amod      _      _
8      ideal      ideal      ADJ      JJ      Degree=Pos    9      amod      _      _
9      domain      domain      NOUN    NN      Number=Sing    10      compound      _      _
10     K      K      PROPN    NNP      Number=Sing    4      nmod      _      _
11     .      .      PUNCT    .      _      1      punct      _      SpacesAfter=\r\n\r\n
```

```
$ cut -f3,4 godement.conllu | grep ADJ
```

Probing the existing lexicon

```
# file adjs.txt  
explicit  
implicit  
elegant  
hard  
connected
```

```
$ RunInformath -unknown-words adjs.txt >unadjs.txt
```



Out of the box
.dk

Symbol table for formal constants
.dkgf, LaTeX

New words
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Syntax Rules, NLG, Dedukti
GF + Haskell

GF RGL

GF + dkgf

```
abstract MySyntax = Categories ** {  
  fun InverseIf : Prop -> Prop -> Prop ;  
}
```

```
concrete MySyntaxEng = CategoriesEng **  
  open GrammarEng, SyntaxEng in {  
    lin InverseIf A B = SSubjS A if_Subj B ;  
  }
```

```
# file mysyntax.dkgf
```

```
#SEMANTICS InverseIf A B = IfProp B A
```

```
#NLG IfProp A B = InverseIf B A
```

GF + dkgf (special case)

```
abstract MySyntax = Categories ** {  
  fun InverseIf : Prop -> Prop -> Prop ;  
}
```

```
concrete MySyntaxEng = CategoriesEng **  
  open GrammarEng, SyntaxEng in {  
    lin InverseIf A B = SSubjS A if_Subj B ;  
  }
```

```
# file mysyntax.dkgf
```

```
#SEMANTICS InverseIf A B = IfProp B A
```

```
#NLG IfProp A B = InverseIf B A
```

Restriction: flat linear patterns on the left hand side (compositionality)

GF + Haskell (general case)

```
abstract MySyntax = Categories ** {  
  
fun AndAdj : Adj -> Adj -> Adj ;  
}
```

```
concrete MySyntaxEng = CategoriesEng **  
  open GrammarEng, SyntaxEng in {  
  
lin AndAdj A B = mkAP and_Conj A B ;  
}
```

```
# file Informath2MathCore.hs
```

```
sem (AdjProp (AndAdj A B) x) = AndProp (AdjProp A x) (AdjProp B x)
```

```
# file MathCore2Informath.hs
```

```
aggregate (AndProp (AdjProp A x) (AdjProp B y)) | x == y = AdjProp (AndAdj A B) x
```

After this: compile both Informath.pgf and RunInformath.hs

Conclusion

Knowledge and tools needed at each level

dkgf:

- how to express concepts in natural language
- RunInformath binary, unix-like shell

gf:

- how to define words in GF by using its libraries
- the GF grammar compiler and Resource Grammar Library

hs:

- hs: how to define recursive traversals in right order and right conditions
- a Haskell compiler (ghc)

Moving things higher up the stack

Goal: to make Informath more accessible, more adaptable, and easier to deploy

Method: by extending the expressivity of dkgf

- first, just GF lexical functions
- second, arbitrary GF functions
- third: natural language examples
- fourth: latex macros
- fifth: #SEMANTICS definitions
- sixth: #NLG definitions
- seventh: \$ notation for automatically generated macros
- TODO: more powerful #SEMANTICS and #NLG

More automation

Goal: to speed up deployment without loss of quality

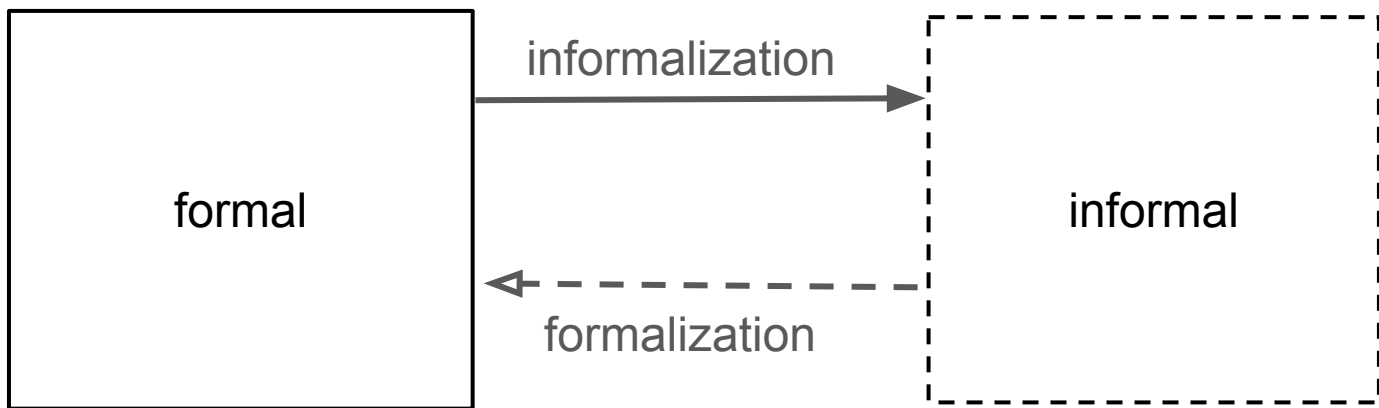
Ideas:

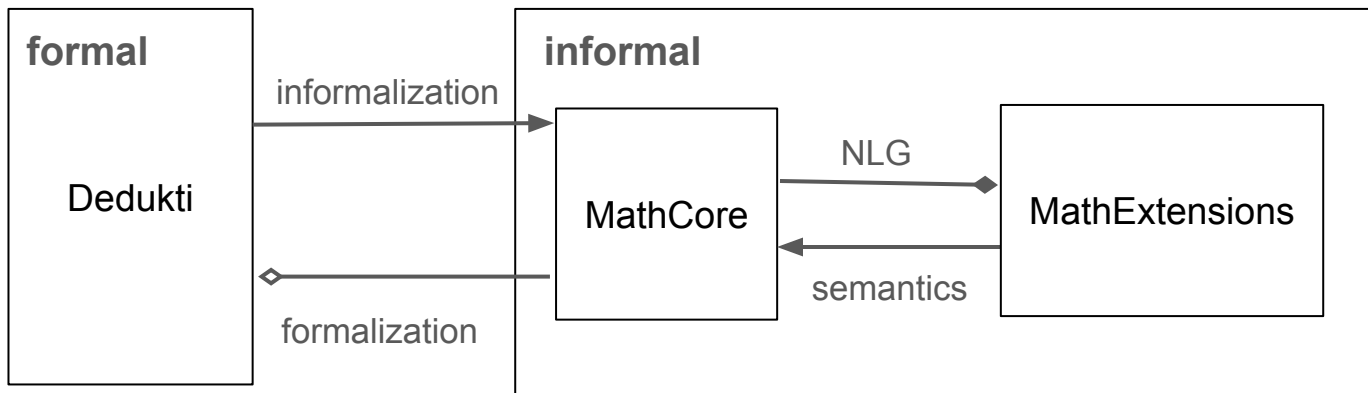
- Symbol table and grammar building as a by-product of LLM autoformalization
- LLM-based ranking of NLG results

Idea from Paul-André Melliès at the MALINCA workshop: when informalizing the result of autoformalizing, choose the informalization that is as close to the original text as possible. In this way, you will get a machine-checked minimally revised version of the text.

This Is Not

The End





.dk

Div x 9

.tex

x is divisible by 9

$\divisible{x}{9}$

.dkgf

```
Div : "X is divisible by Y" | \divisible
#MACRO \newcommand{divisible}[2]{#2 \mid #1}
```

.gf abstract

```
fun
  divisible_Adj : Adj
  by_Prep : Prep
```

.gf English

```
lin
  divisible_Adj = mkAdj "divisible"
  by_Prep = RGL.by_Prep
```

German

```
divisible_Adj = mkAdj "teilbar"
by_Prep = RGL.by_Prep
```